2022 John O'Bryan Mathematics Competition 5-Person Team Test

Abbreviated Instructions: Answer each of the following questions using separate sheet's of paper. Questions will not be scored without the following two items:

| | • Place you | ar team code in the up | pper right corner (| of each page that | t will be turned | in. |
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| 7111 | den takes a mathematics test consisting of 100 questions, where the answer to each sestion is either TRUIF or FAUSE. For every five consequeive questions on the test the | |
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| an | swers to exactly three of the questions are TRUE. If the answers to Question 1 and | |
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| a. | Find the number of questions on the test for which the correct answer is TRUE. | |
| | Find the number of questions on the test for which the correct answer is TRUE. Find the correct answer to the sixth question on the test. | |
| b. | | ł |
| b. | Find the correct answer to the sixth question on the test. | |
| b. | Find the correct answer to the sixth question on the test. | |

2022 John O'Bryan Mathematical Competition Freshman-Sophomore Individual Test



- 5. Let $x^2 4y^2 = 30$ and x 2y = 5. Determine the value of (x + 2y).
- 6. The sum of twice a number and three times a second number is 16. The difference between the two numbers is 3. If the first number is greater than the second number, determine the sum of the two numbers.
- 7. Circle P has diameter \overline{AB} . $\triangle ABC$ is isosceles with base \overline{BC} intersecting the circle at point D. AC = 4 and DC = 1. Determine the numeric area of $\triangle ABC$. Give your answer as a radical expression (in the form $a\sqrt{b}$), where b is a whole number as small as possible.
- 8. In a circle with center C, minor arc $\triangle AB$ has length $\frac{8\pi}{9}$. $\angle ACB = 40^{\circ}$. Determine the radius of the circle C.
- 9. Let $k = 110 + 110 + 110 + 110 \dots$. Determine the exact value of k.
- 10 Let b and c be integers with $g(x) = x^2 + bx + c$ and $f(x) = x^2 + cx + b$. Determine the sum (b + c) when g(c) = f(b) and $c \ne b$.

| . A square with nume | ric area k is inscribed in a semicircle | (two vertices of the square lie of | n the semicircle |
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Name:

Team Code:

2022 John O'Bryan Mathematical Competition Freshman/Sophomore Individual Test

Note: All answers must be written legibly in the correct blanks on the answer sheet and in simplest form. Exact answers are to be given unless otherwise specified in the question. No units of measurement are required. Each problem has the same point-value.

1. 11.

2. 12.

3. 13.

4. 14.

5. 15.

6. 16.

7. 17.

8. 18.

9. 19.

10. 20.

| Name: | ANSWERS |
|-------|----------------|
| | |

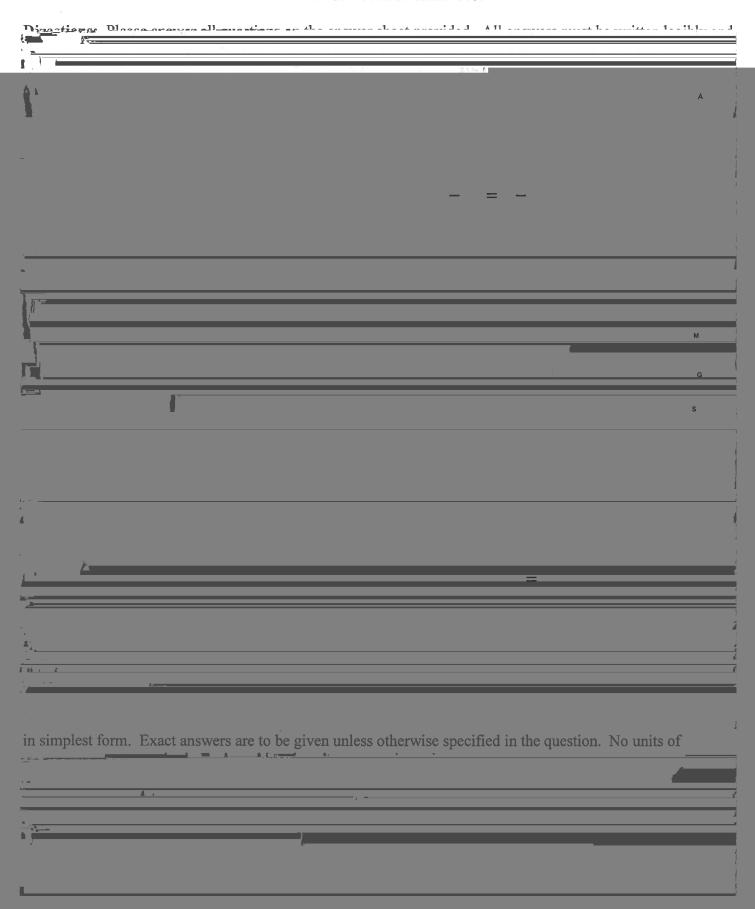
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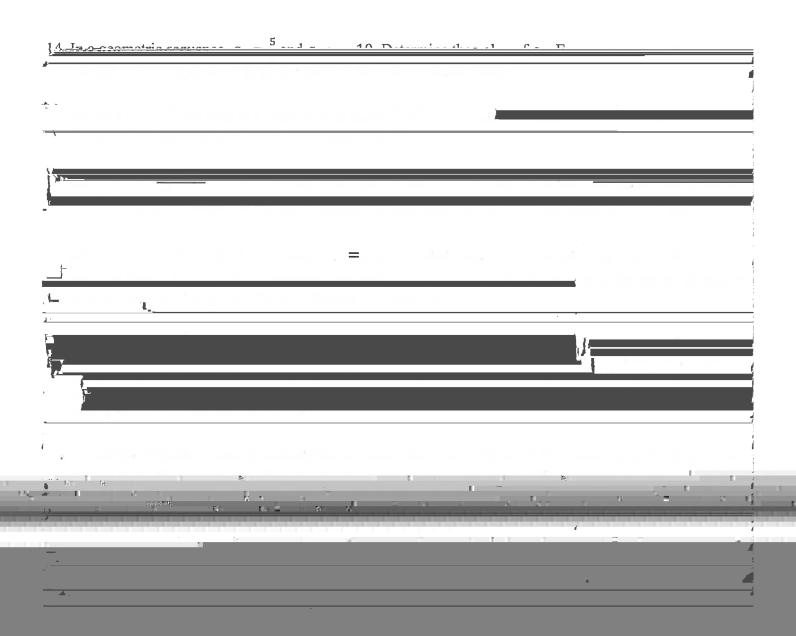
2022 John O'Bryan Mathematical Competition Freshman-Sophomore Individual Test

Note: All answers must be written legibly and in simplest form. Exact answers are to be given unless

| 1. | | | 11. | | |
|----|---------------|-----------------------------|-----|---------------|---------------------------------------|
| 2. | 640 | | 12. | 4850 | |
| 3. | 1 | W | 13. | 11 | |
| 4. | 18 | reduced common fraction. | 14. | <u> </u> | Must be this |
| 5. | 6 | | 15. | 2√61 | Must be this exact answer. |
| 6. | 7 | | 16. | $\frac{1}{2}$ | Must be this reduced common fraction. |
| 7. | $\sqrt{15}$ | Must be this exact answer. | 17. | 8 | |
| 8. | 4 | | 18. | 1.457 | Must be this decimal. |
| 9. | 11 | | 19. | 88.443 | Must be this decimal. |
| 10 | -1 | | 20 | 3560 | |

2022 John O'Bryan Mathematical Competition Junior-Senior Individual Test





| Name: | Team Code: |
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2022 John O'Bryan Mathematical Competition

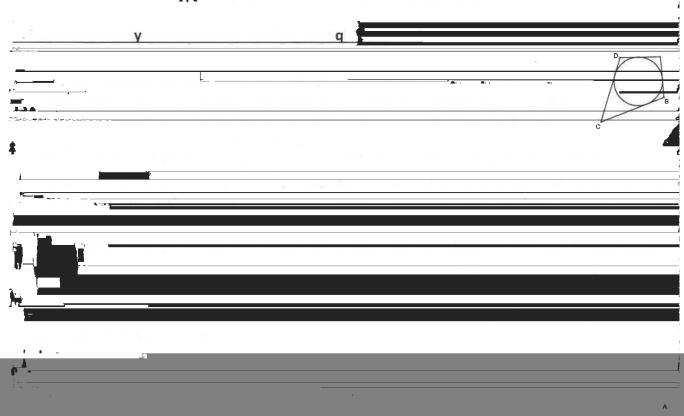
| | Junior/Senior Inc | |
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| Note: | All answers must be written legibly in the correc | t blanks on the answer sheet and in simplest form. necified in the auestian. No units of measurement |
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2022 John O'Bryan Mathematical Competition Junior-Senior Individual Test

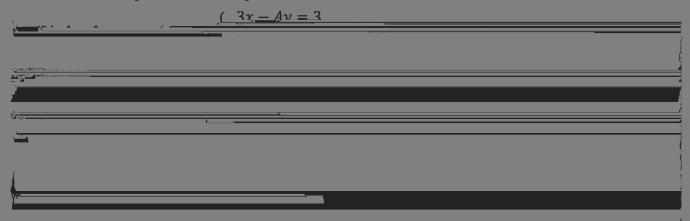
Note: All answers must be written legibly and in simplest form. Exact answers are to be given unless

| | / . = | Must be this | | | |
|-----|-------------------------------|----------------------------------|-----|---------------|--------------------------------|
| 3. | 24 | | 13. | -3/2 | Must be this reduced fraction. |
| | | | 14. | | |
| 5. | $2\sqrt{61}$ | Must be this radical expression. | 15. | 3560 | |
| 6. | 2 | | 16. | 0 or zero | |
| 7. | 8 | | 17. | 5/2 | Recorded to |
| 8. | -15 | | 18. | 0.375 or .375 | Must be this decimal. |
| 9. | $i-1 \text{ or } \sqrt{-1}-1$ | Must be one of these. | 19. | 2:5 | Must be this exact ratio. |
| 10. | 14 | | 20. | 40/0 | Must be this |

2022 John O'Bryan Mathematical Competition Questions for the Two-Person Speed Event



1. A system of equations has $x^2 - 4y^2 = 30$ and x - 2y = 5 and k = x + 2y. Quadrilateral *ABCD* is circumscribed about a circle with side lengths BC = 20 and AD = 17. The perimeter of the quadrilateral is w. Determine the value of k + w.



| Names: | School: |
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2022 John O'Bryan Mathematical Competition Two-Person Speed Event

Note: All answers must be written legibly and in simplest form. Exact answers are to be given unless

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7.

8.

SCORE

T1.

T2.

| Names: | School: |
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2022 John O'Bryan Mathematical Competition Answers for the Two-Person Speed Event

Note: All answers must be written legibly and in simplest form. Exact answers are to be given unless otherwise specified in the question. No units of measurement are required. Each problem has the same point-value.

| 1 | 80 | SC | Calculators are not allowed to be used on the first four questions! |
|-----|------|---------------------------------------|---|
| 2. | -9 | · · · · · · · · · · · · · · · · · · · | This competition consists of eight competitive rounds. Correct answers will receive the following |
| 3. | 9.0 | "Degrees" optional | 1 st : 7 points 2 nd : 5 points |
| 4. | 9 | | |
| 5. | 294 | | 4 |
| 6. | 1000 | | There is a three minute time limit |
| 7. | | at be this reduced mon fraction | |
| 8. | 23 | | SCORE |
| T1. | 69 | | |
| Т2. | 24 | | |