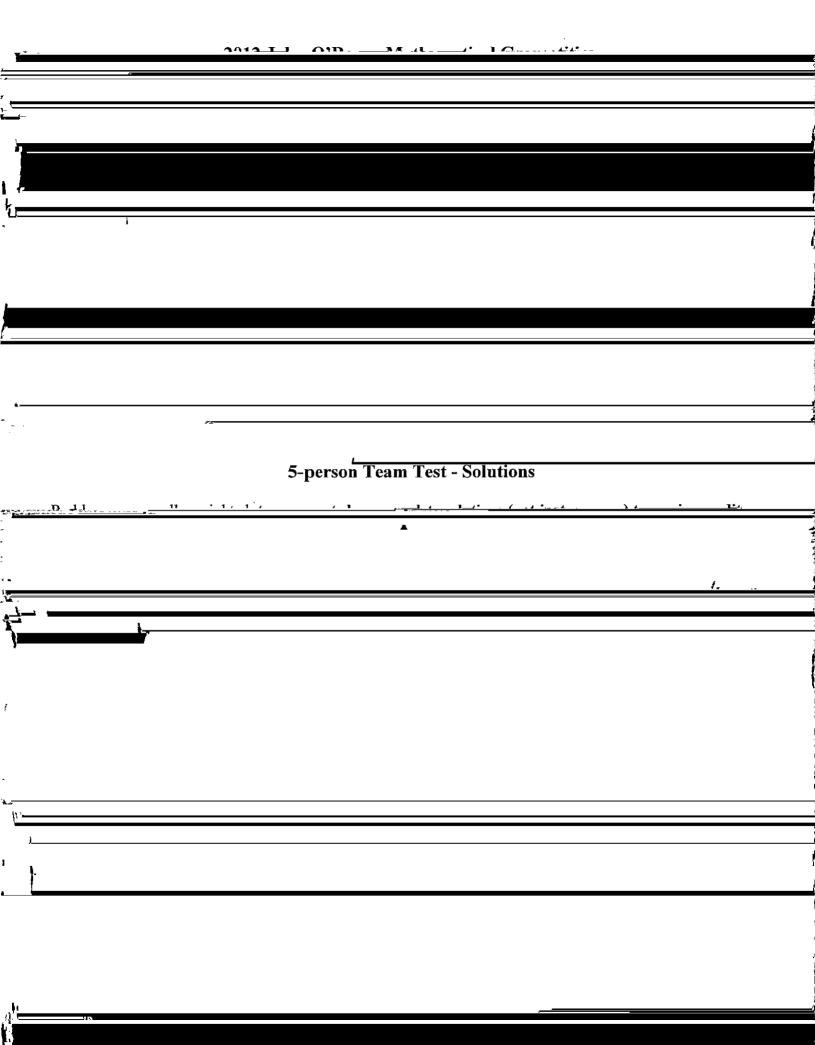
|            | 7012 John O'Prune Mathematical Compatition   |
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|            | 5-person Team Test   |
| n<br>to    | abbreviated Instructions: Answer each of the following questions using separate sheet(s) of paper for each umbered problem. Place your team letter in the upper right corner of each page that will be turned in (failure of do this will result in no score). Place problem numbers in the upper left corner. Problems are equally reighted: teams must show complete solutions (not just answers) to receive credit. More specific |
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| 5. Given four v | rertices, a "graph" is create | a by joining any number | er of the vertices by s | araigni ime(s). Two    |
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says that B\_Y matches and the word is BAY. But then SAY is not Odd. So niether the A nor the Y match. So we get S must match from SAY. From the other two Odds we get either SEE or SUN. But BUY is even and so only SEE is left as a possibility.

3. Inscribe a rectangle of base *b* and height *h* in a circle of radius 1, and inscribe an isosceles triangle in a region of the circle cut off by one base of the rectangle (with that base becoming also one side of the triangle). For what value(s) of *h* can one construct these shapes as described such that the rectangle and triangle have the same area?

This can be interpreted in two ways, either as the solid triangle shown in the picture or as the triangle formed from the two dotted lines and the base of the rectangle.

Let b be the base of the rectangle and b be its height.

Using the triangle including the dotted lines, since the diameter is 2, the height of the triangle is  $\frac{1}{2}(2-h) = 1-h$ /2. Thus the area of the triangle is  $\frac{1}{2}(b)(1-h/2)$ . Setting this equal to the area of the rectangle bh, we find h = 2/5.

